

# 4728 Mechanics 1

|      |   |   |  |  |
|------|---|---|--|--|
| 1    | $70 \times 9.8$ or $70g$<br>$70 \times 0.3$<br>$686 + 21$<br>$707 \text{ N}$  | B1<br>B1<br>M1<br>A1<br>[4]             | =686<br>=21<br>+ cvs [70(9.8+0.3) gets B1B1M1]   |  |
| 2    | $+/- (40 \times 4 - 60 \times 3)$<br>$+/- ([40 + 60] v$<br>$+/- (40 \times 4 - 60 \times 3) = +/-(40 + 60) v$<br>Speed = $0.2 \text{ ms}^{-1}$<br><br>Same as heavier or opposite lighter/"she" | B1<br>B1<br>M1<br>A1<br>B1<br>[5]       | Difference of terms, accept with g<br>Sum of terms, accept with g.<br>Accept inclusion of g in equation.<br>Not if g used. $SR$ $40 \times 4 - 60 \times 3 = [40 + 60] v$ ;<br>$v=0.2$ , as heavier, award 5 marks<br>"Left" requires diagram for B1<br>If same direction before collision award<br>B0B1M1A0B0 |  |
| 3i   | $\sqrt{(12^2 + 15^2)}$<br>$19.2 \text{ N}$<br><br>$\tan\theta = 12/15$ , $\tan\theta = 15/12$ , $\sin\theta = 12/19.2$ , $\cos\theta = 15/19.2$<br>Bearing = $038.7^\circ$                      | M1<br>A1<br>A1<br>M1<br>A1<br>A1<br>[6] | Applies Pythagoras, requires +.<br><br>trig and R included between X and Y<br>Accept cv 19.2<br>Accept 039 or 39 or art 39 from below<br>(not given if X and Y transposed)<br>ft cv 19.2<br>$180 + cv 38.7 (-360)$ or correct answer   |  |
| 3ii  | $E = 19.2$<br>Bearing = $180 + 38.7 = 219^\circ$  | B1ft<br>B1ft<br>[2]                     |  |  |
| 4i   | $v = dx/dt$<br>$v = 4t^3 - 8x2t$<br>$v(2) = 4x2^3 - 8x2x2$<br>$= 0$<br>$x(2) = 2^4 - 8x2^2 + 16 = 0$  | AG<br>AG<br>[5]                         | M1<br>A1<br>M1<br>A1<br>B1<br>[5]  | Uses differentiation, may be seen in (ii)<br>Accept with +c<br>Substitutes 2 in cv v, explicit<br>A0 if +c<br>Substitutes 2 in displacement, explicit                                |
| 4ii  | $a = dv/dt$<br>$a = 12t^2 - 16$<br>$a(2) = 12x2^2 - 16 = 32 \text{ ms}^{-2}$  | AG<br>AG<br>[3]                         | M1<br>A1<br>A1<br>[3]  | Uses differentiation of v formula<br>Accept with +c<br>A0 with +c  |
| 5ia  | $250a = -150$<br>$a = -0.6 \text{ ms}^{-2}$   | AG<br>[2]                               | M1<br>A1<br>[2]  | Values used in N2L for trailer F = +/- 150<br>Or -ve convincingly argued   |
| 5ib  | $900 \times -0.6 = D - 600$ or $(900+250)x-0.6 = D - 600 - 150$<br>$D = 60 \text{ N}$   | [3]                                     | M1<br>A1<br>A1<br>[3]  | Applies N2L to car or car/trailer with<br>correct number of forces<br>(including T if T=0 used later)  |
| 5ic  | $15^2 = 18^2 + 2x(-0.6)s$<br>$s = 82.5 \text{ m}$   | [2]                                     | M1<br>A1<br>[2]  | Uses $v^2 = u^2 + 2(+/-0.6)s$ with 15, 18<br>Positive, allow from $18^2 = 15^2 + 2x0.6s$   |
| 5iia |   | M1<br>[2]                               |  | Applies N2L to car+trailer with F(driving)<br>F(resisting), F(wt cmpt-allow without g),<br>or each part, as above and T.   |
| 5iib | $(900+250)a = 980 - 600 - 150$<br>$+ /-(900+250)x9.8\sin3$<br>$a = 0.713 \text{ ms}^{-2}$<br><br>$250 \times 0.713 = T - 150 + 250 \times 9.8\sin3$<br><br>$T = 200 \text{ N}$                  | A1<br>A1<br>A1<br>[4]                   | M1<br>A1<br>A1<br>[4]  | $900a = 980 - 600 +/- 900 \times 9.8 \sin 3 - T$<br>$250a = T - 150 +/- 250 \times 9.8 \sin 3$<br>Allow (art) 0.71 from correct work   |
|      |   |   | M1<br>A1<br>A1<br>[3]  | N2L for trailer, cv a, with correct number<br>of forces of correct type. Or for car<br>$900 \times 0.713 = -T - 600 + 900 \times 9.8 \sin 3 + 980$<br>Anything rounding to 200 (3sf) |

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| 6i   | $4.9 = \mu \times 14.7$<br>$\mu = 1/3$  | AG | M1<br>A1<br>[2]                   | Uses $F = \mu R$<br>Allow 0.333 or 0.3 recurring   |
| 6iia | $R + 4.9\sin 30 = 14.7$<br>$R = 12.25 \text{ N}$<br>$F = 12.25 \times 1/3$<br>$F = 4.08(333..) \text{ N}$ [or $49/12 \text{ N}$ ]               |    | M1<br>A1<br>A1<br>M1<br>A1<br>[5] | 3 force vertical equation<br>Accept 12.2 or 12.3<br>Uses $F = \mu R$ with new $R$ {may be seen in part b}        |
| 6iib | $m = 14.7/9.8 = 1.5 \text{ kg}$   |    | B1<br>M1                          | N2L horizontally with 2 relevant forces, including $4.9\sin/\cos 30$   |
| 6iii | $4.9\cos 30 - 4.08(333..) = 1.5a$<br>$a = 0.107 \text{ ms}^{-2}$  |    | A1<br>A2<br>[5]                   | Allow $c(F)$ <b>SR</b> Award A1 if $m=14.7$ used<br><b>SR</b> A1 for 0.11, 0.109<br>or art 0.011 from $m = 14.7$ |
|      | $\mu R = (14.7 - 4.9\cos 30)/3$<br>Horizontal component of force = $4.9\sin 30$<br>Horizontal component of force < $\mu R$<br>Friction = 2.45 N |    | B1<br>B1<br>M1<br>A1<br>[4]       | 3.49, accept 3.5<br>2.45, accept 2.4 or 2.5<br>Comparing two values<br>Not 2.4 or 2.5; Explicit (M1 essential)   |

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| 7i   | $s = 0.5 \times 1.4 \times 0.8^2$<br>$s = 0.448 \text{ m}$<br>$v = 1.4 \times 0.8$<br>$v = 1.12 \text{ ms}^{-1}$                   |  | M1<br>A1<br>M1<br>A1<br>[4]  | Uses $s = 0.5 \times 1.4t^2$<br>Not 0.45<br>Uses $v = 1.4t$   |
| 7ii  | $0^2 = 1.12^2 - 2 \times 9.8s$<br>$s = 0.064 \text{ m}$<br>$0 = 1.12 - 9.8t$ (t = 0.114s)<br>$t = (0.114 + 0.8) = 0.914 \text{ s}$ |  | M1<br>A1<br>M1<br>A1<br>[4]  | Uses $0^2 = u^2 - 2gs$ or $u^2 = 2gs$<br>Allow verification<br>or $0.064 = 1.12t - 4.9t^2$<br>Allow 0.91 {or 0 = 1.12t - 4.9t <sup>2</sup> and halve t} |
| 7iii | Scalene triangle, base on t axis<br>right edge steeper and terminates on axis, or crosses axis at t = 0.91                         |  | B1<br>B1<br>[2]              | NB Award A1 for 0.91 on t axis if total time not given in (ii)  |
| 7iv  |  |  | M1<br>A1<br>A1<br>[2]        | Uses N2L for A or B with attempt at 2 forces<br>Either  |
| 7va  | $1.4xA = 9.8xA - 5.88$ or $1.4xB = 5.88 - 9.8xB$<br>$A = 0.7$<br>$B = 0.525$   |  | A1<br>A1<br>A1<br>[4]        | Not 0.53  |
| 7vb  | $T = 0.5 \times 9.8 + 2 \times 5.88$<br>$T = 16.66 \text{ N}$<br>$T = 4.9 \text{ N}$   |  | M1<br>A1<br>[2]<br>B1<br>[1] | Uses tension and 0.5g without particle weights<br>Allow 16.7  |